

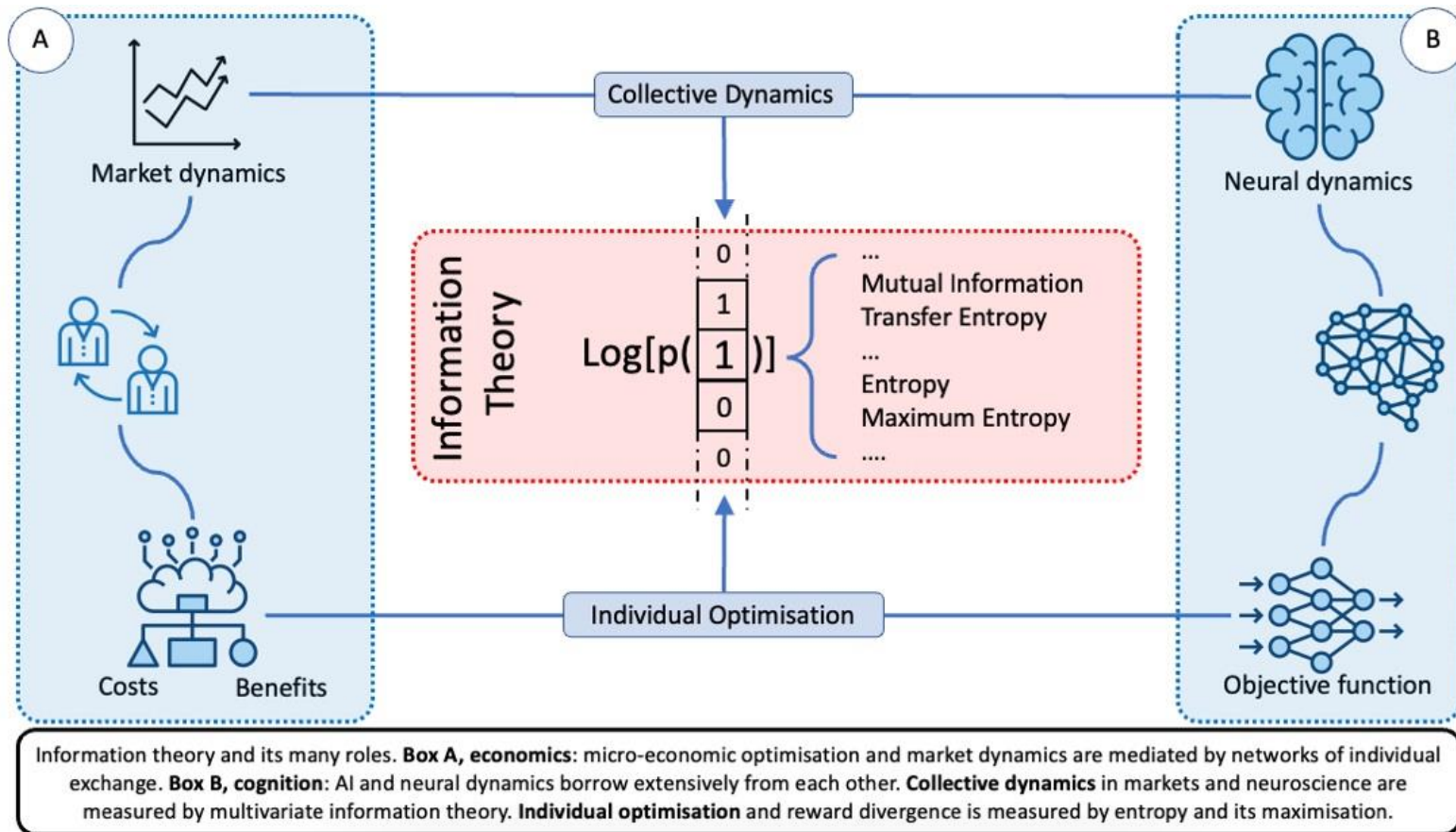
Critical Risks and Opportunities of AI, Economics, and Social Network Theory

Dr. Michael Harré
Modelling and Simulation Group
School of Computer Science
University of Sydney

“Complexity, Criticality and Computation”
Symposium C³ January 2023



Silicon Intelligence : Economics : Psychology



Information Theory for Agents in Artificial Intelligence, Psychology, and Economics

by Michael S. Harré

Complex Systems Research Group, Faculty of Engineering, The University of Sydney, Sydney 2006, Australia

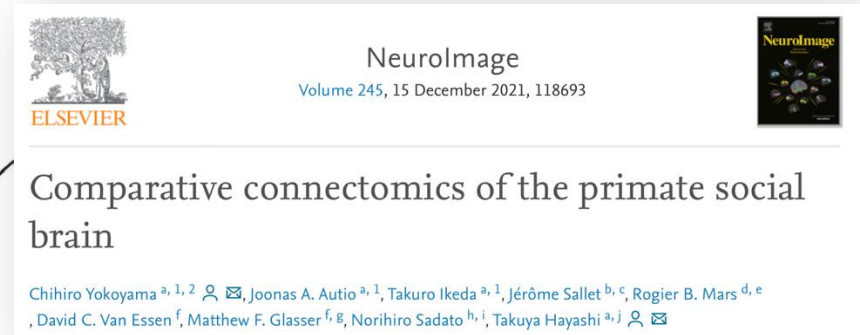
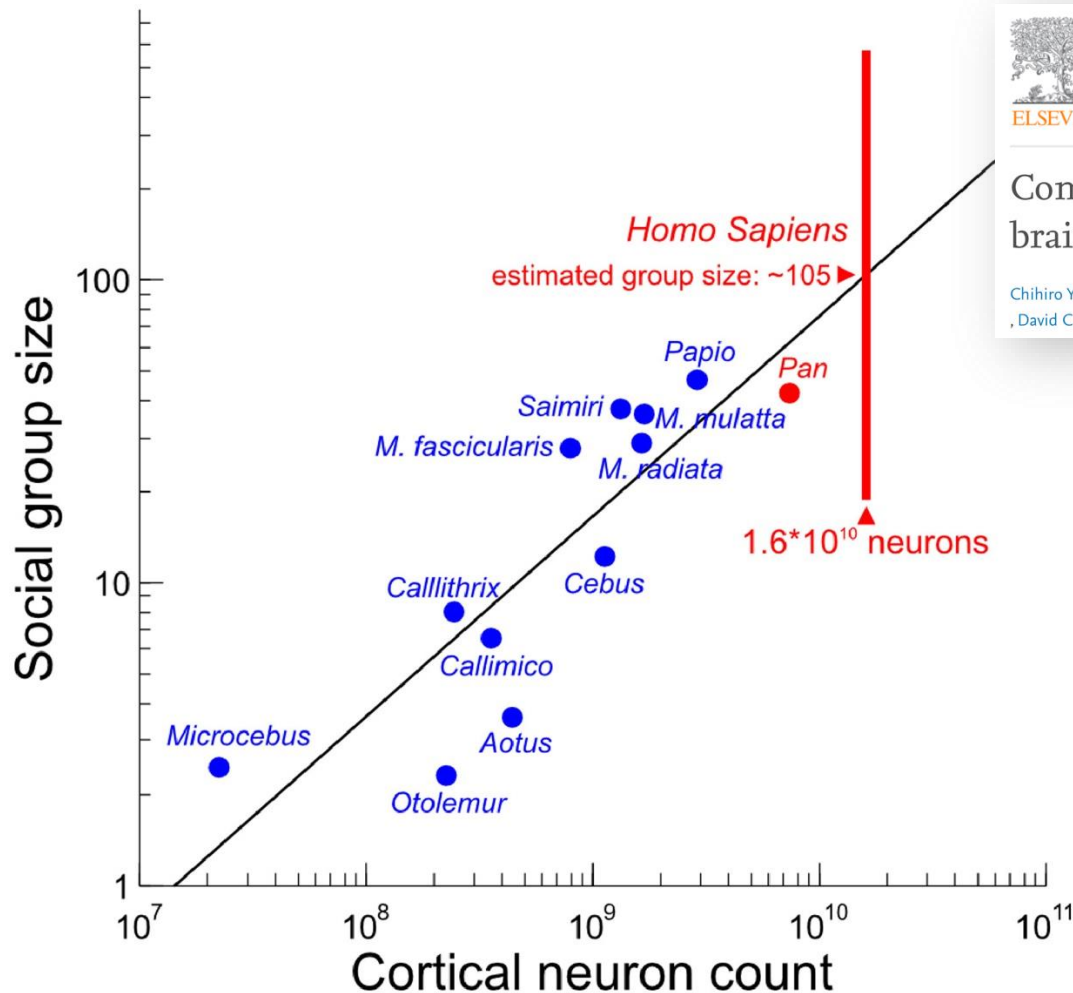
Entropy 2021, 23(3), 310; <https://doi.org/10.3390/e23030310>

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3. Cicero's Free Energy for 'Game Theory of Mind'
4. Consequences of 'Game Theory of Mind' for AI



1. Motivating Theory of Mind for Social Networks



1. Motivating Theory of Mind for Social Networks



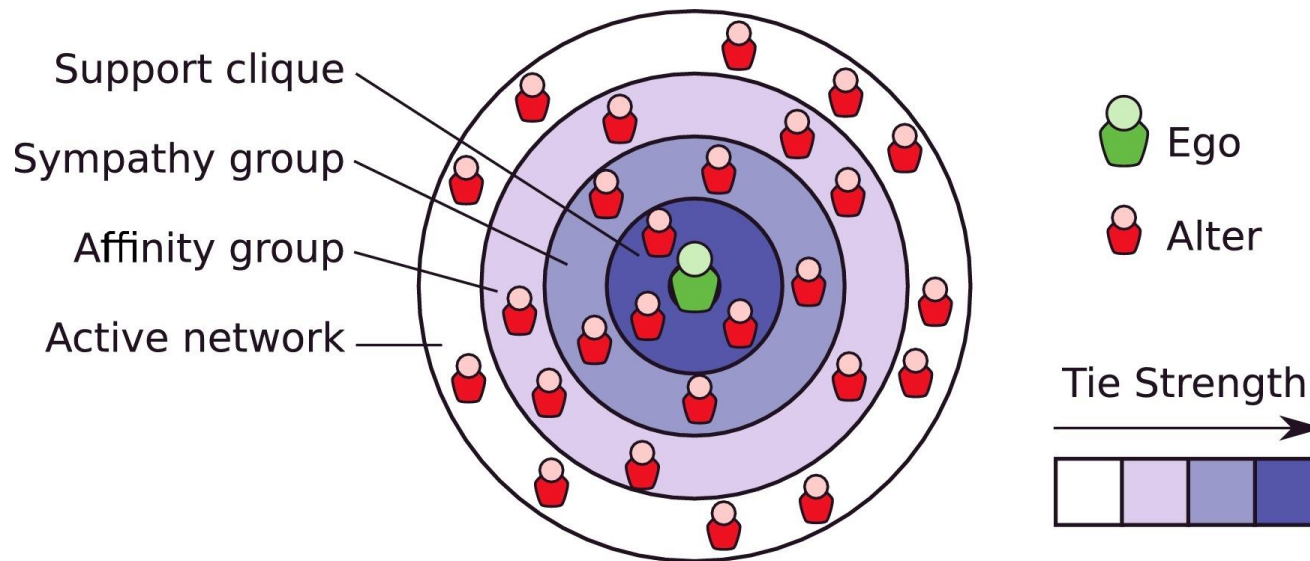
Computer Communications

Volume 76, 15 February 2016, Pages 26-41



Ego network structure in online social networks and its impact on information diffusion

Valerio Arnaboldi , Marco Conti , Massimiliano La Gala , Andrea Passarella , Fabio Pezzoni



1. Motivating Theory of Mind for Social Networks

INTERFACE

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Research

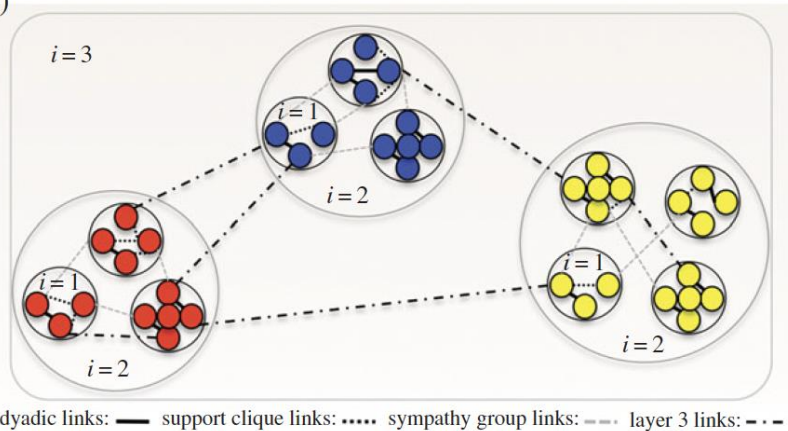


The social brain: scale-invariant layering of Erdős–Rényi networks in small-scale human societies

Michael S. Harré and Mikhail Prokopenko

Complex Systems Research Group, Faculty of Engineering and IT, The University of Sydney, Sydney, Australia

(a)



(b)

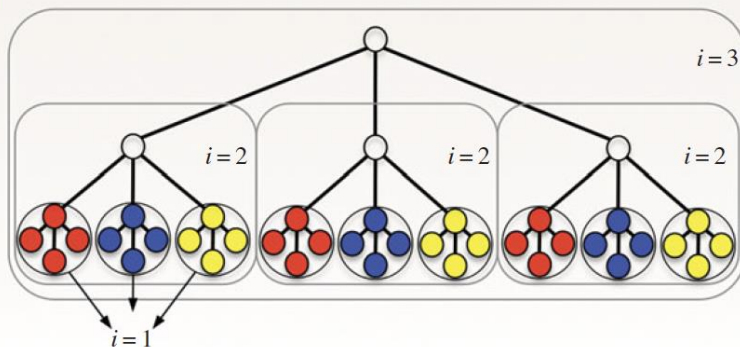


Figure 1. Two different social network models. (a) Random links form between sub-group members. As the average number of links per person increases in discrete steps, the network size also increases in predictable, discrete, steps. (b) A structured hierarchy similar to modern military, bureaucratic and corporate structures in which each layer is ‘managed’ by a coordinator. (Online version in colour.)

1. Motivating Theory of Mind for Social Networks

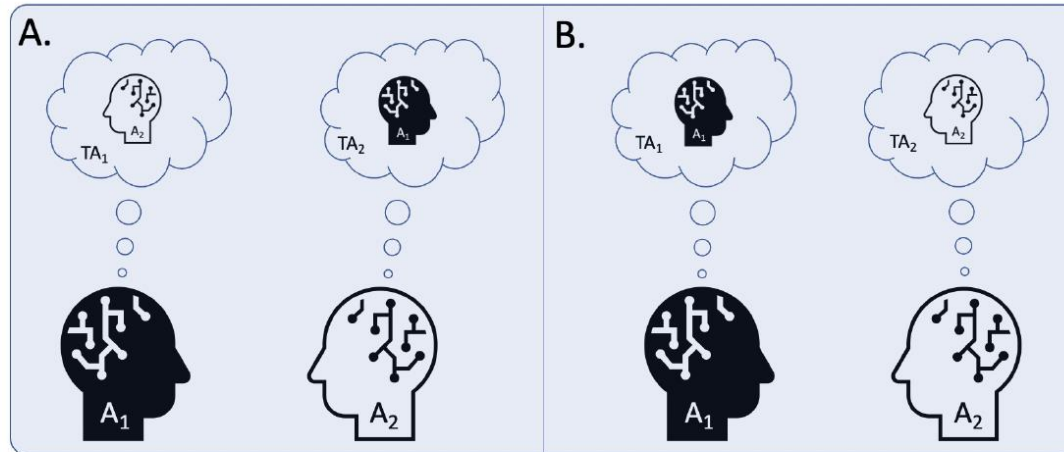


Figure 2. Left: Both agents A_1 and A_2 have a representation of the other agent's cognition (ToM). Right: Both agents have a representation of their own cognition (introspection). TA_i is a cognitive space (see for example [15,16]) in which the 'thoughts of agent i ' occur.

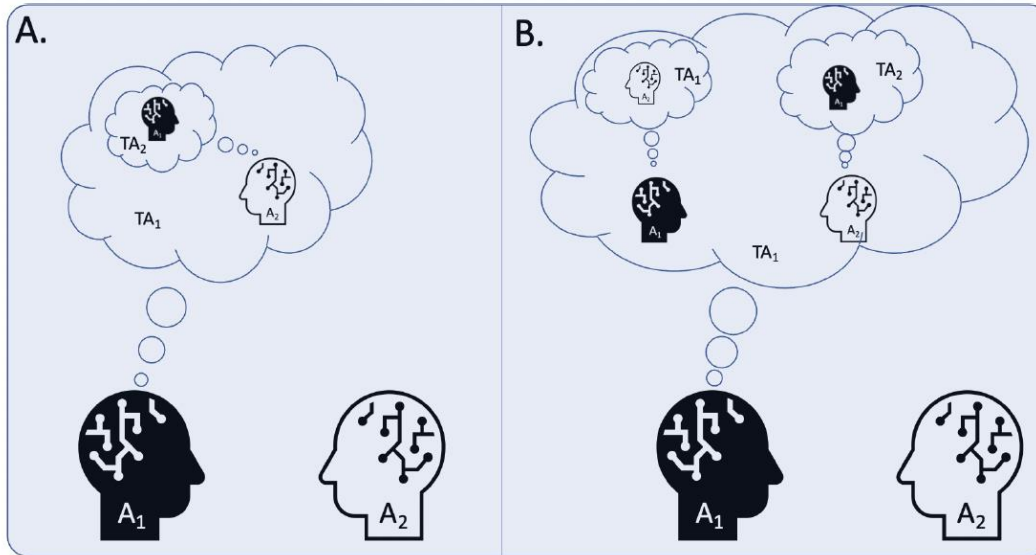
The role of metacognition in human social interactions

Chris D. Frith ✉

Published: 05 August 2012

<https://doi.org/10.1098/rstb.2012.0123>

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The role of metacognition in human social interactions

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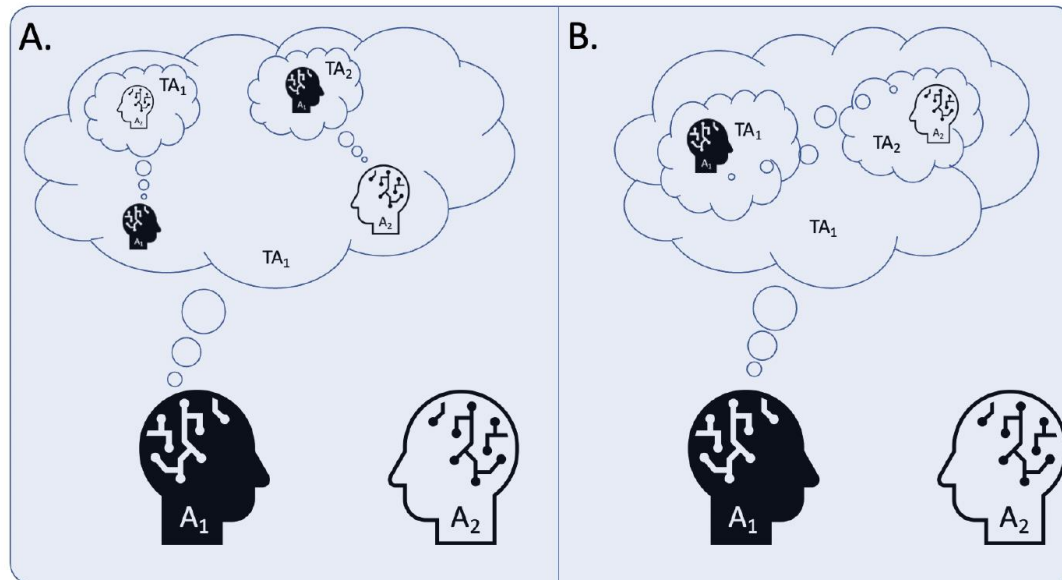
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Game Theory of Mind

Wako Yoshida , Ray J. Dolan, Karl J. Friston

Published: December 26, 2008 • <https://doi.org/10.1371/journal.pcbi.1000254>

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The University of Sydney

What Can Game Theory Tell Us about an AI 'Theory of Mind'?

by Michael S. Harré

Complex Systems Research Group, Faculty of Engineering, The University of Sydney, Sydney 2006, Australia

Games **2022**, *13*(3), 46; <https://doi.org/10.3390/g13030046>

Received: 30 April 2022 / Revised: 30 May 2022 / Accepted: 16 June 2022 / Published: 20 June 2022

Game Theory of Mind

Wako Yoshida , Ray J. Dolan, Karl J. Friston

Published: December 26, 2008 • <https://doi.org/10.1371/journal.pcbi.1000254>

2. Free Energy Principles of Decision Theory

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Free Energy, Free Utility:

$$\left. \begin{aligned} H(p) &= - \sum_x p(x) \log(p(x)) \\ V(p) &= \text{internal energy (potential function)} \\ \mathcal{F}(p) &= V(p) - T H(p) \quad (\text{where } T \text{ is temperature}) \end{aligned} \right\} \text{Helmholtz Free Energy} \quad (1)$$

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$$\left. \begin{aligned} H(P) &= - \sum_{x,y} P(x,y) \log(P(x,y)) \\ U_a(P) &= E_p[U_a(x,y)] \quad (\text{expected utility for } a) \\ \mathcal{F}(P) &= U_a(P) - T H(P) \quad (T \text{ is uncertainty or error}) \end{aligned} \right\} \text{Free Utility (2 players)} \quad (2)$$

Strategic Choice of Preferences: the Persona Model

David Wolpert, Julian Jamison, David Newth and Michael Harre

From the journal *The B.E. Journal of Theoretical Economics*

<https://doi.org/10.2202/1935-1704.1593>

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 \end{aligned} \right\} \text{Free Utility (2 players) (2)}$$

Optimising these "free functionals" leads to standard exponential solutions:

$$\begin{aligned}
 P(x) &\propto \exp(-\beta V(P)) \\
 P(x | x = x_i) &\propto \exp(\beta U_a(P(y) | x = x_i)) \\
 P(y | y = y_i) &\propto \exp(\beta U_b(P(x) | y = y_i))
 \end{aligned}$$

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2. Free Energy Principles of Decision Theory

[Published: 13 January 2010](#)

The free-energy principle: a unified brain theory?

[Karl Friston](#)

[Nature Reviews Neuroscience](#) **11**, 127–138 (2010) | [Cite this article](#)

Friston's Free Energy Principle:

One of the goals of Friston's work is to estimate the joint probability of states observed o and actual states s via Bayes Theorem:

$$P(s, o) = P(o|s)P(s)$$

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This calculation is often too difficult to compute directly so Friston's "Free Energy Principle" for the brain addresses this by estimating an alternative probability $Q(s)$ via optimisation:

$$Q^*(s) = \underset{Q(s)}{\operatorname{argmin}} \mathcal{F}(Q) \quad (3)$$

$$Q^*(s) \simeq P(s|o) \quad (4)$$

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$$\mathcal{F}(Q) = E_Q[\log(Q(s)) - \log(P(s|o))] \quad (5)$$

$$= \underbrace{E_Q(-\log(P(s|o)))}_{\substack{\text{cross entropy} \\ = \text{expected log loss}}} - \underbrace{H(Q(s))}_{\text{entropy}} \quad (6)$$

2. Free Energy Principles of Decision Theory

The three ideas to take away from this section:

$$\begin{aligned}\mathcal{F}(Q) &= E_Q[\log(Q(s)) - \log(P(s|o))] \\ &= \underbrace{E_Q(-\log(P(s|o)))}_{\text{cross entropy} \\ &\quad = \text{expected log loss}} - \underbrace{H(Q(s))}_{\text{entropy}}\end{aligned}$$

note: Grunwald and Dawid showed that this is a “game” between nature and decision maker (2004)

Game theory, maximum entropy, minimum discrepancy and robust Bayesian decision theory

[PD Grünwald, AP Dawid - the Annals of Statistics, 2004 - projecteuclid.org](#)

$$H(P) = - \sum_{x,y} P(x,y) \log(P(x,y))$$

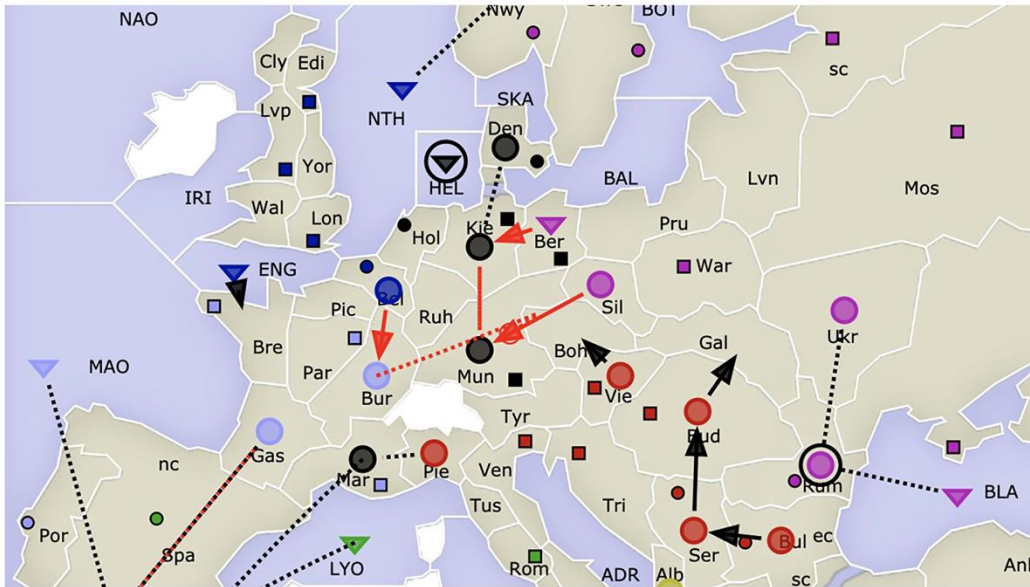
$$U_a(P) = E_p[U_a(x,y)] \text{ (expected utility for } a \text{)}$$

$$\mathcal{F}(P) = U_a(P) - T H(P) \quad (T \text{ is uncertainty or error})$$

Optimising these "free functionals" leads to standard exponential solution

3. Cicero: “Free Energy” for a Game Theory of Mind II

The game of “Diplomacy” and the AI Cicero that learned to play like a human



Diplomacy is a 61-year-old board game about taking over Europe. It's a true classic - highly influential, intensely beloved and widely acclaimed - and the first time I played it, I thought it was rubbish.

In Diplomacy, each player controls one of seven nations at the start of the 20th century, submitting movement orders to their armies and fleets each turn in order to gain new territories and thereby build more troops - the goal being to control 18 of the game's supply cities at the same time. Its rules are simple enough to make Risk look fiendishly difficult and yet, all the same, it is an extremely nuanced game of strategy and cunning. (JFK apparently enjoyed the game, as did Henry Kissinger.)

About Diplomacy

Released: 1959

Players: 2-7

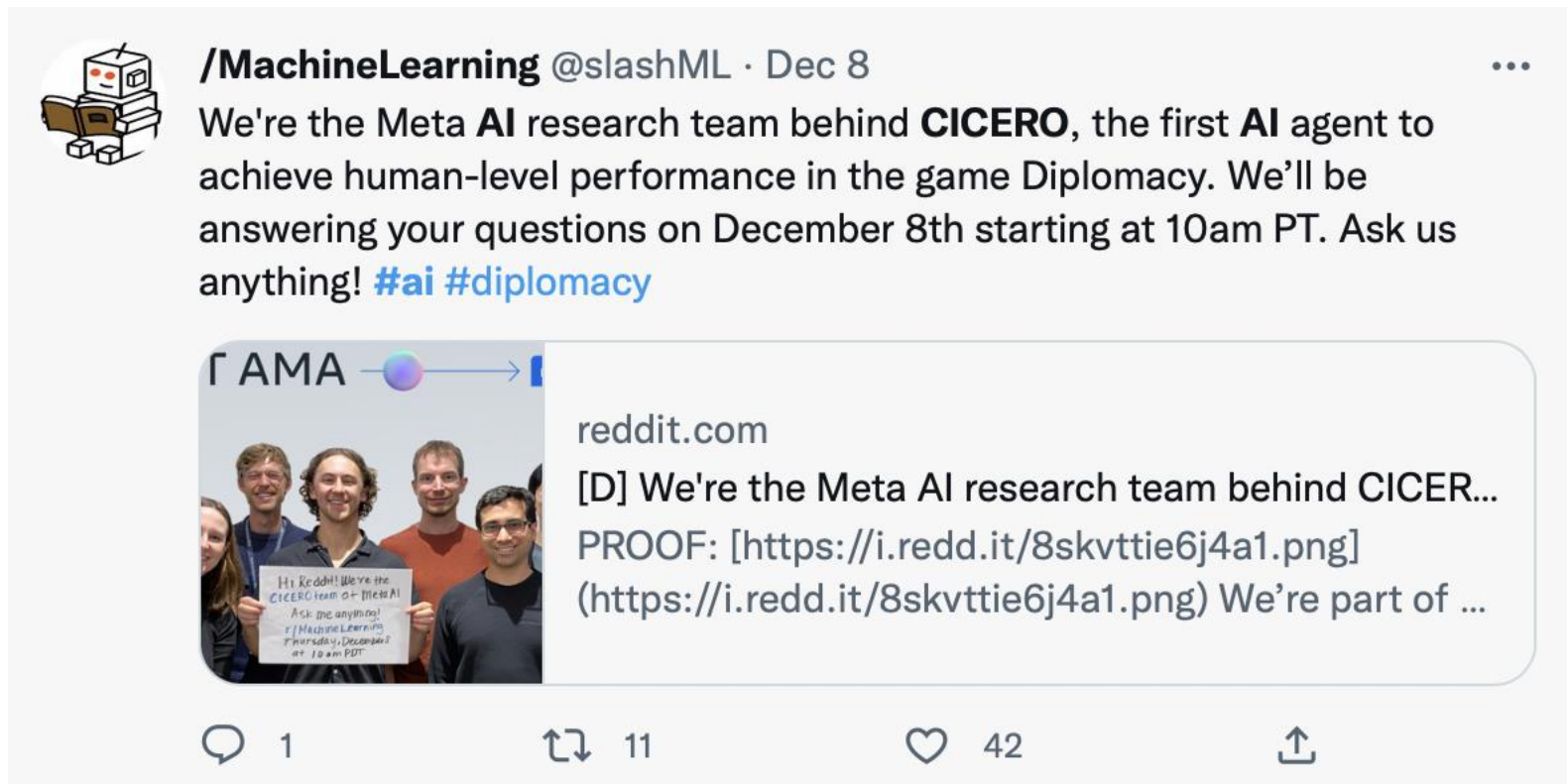
Playing time: 360 mins

Rules complexity: Very low

Strategic depth: High

3. Cicero: “Free Energy” for a Game Theory of Mind II

The game of “Diplomacy” and the AI Cicero that learned to play like a human



3. Cicero: “Free Energy” for a Game Theory of Mind II

The game of “Diplomacy” and the AI Cicero that learned to play like a human



Yann LeCun @ylecun · Nov 23

...

Big **AI** milestone today: **CICERO**, an **AI** agent that can negotiate and cooperates with people.

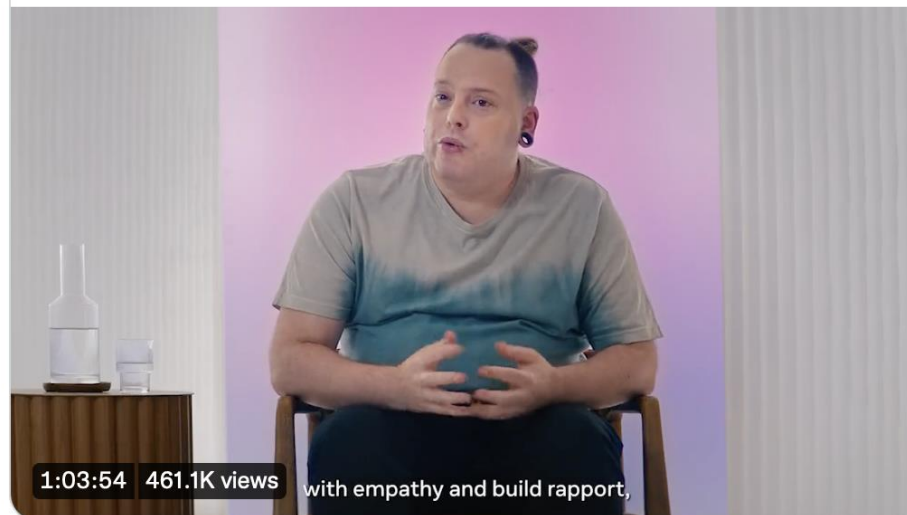
It is the first **AI** system to achieve human-level performance in the popular strategy game Diplomacy.

Cicero ranked in the top 10 of participants on webDiplomacy.net

∞ **Meta AI**  @MetaAI · Nov 23

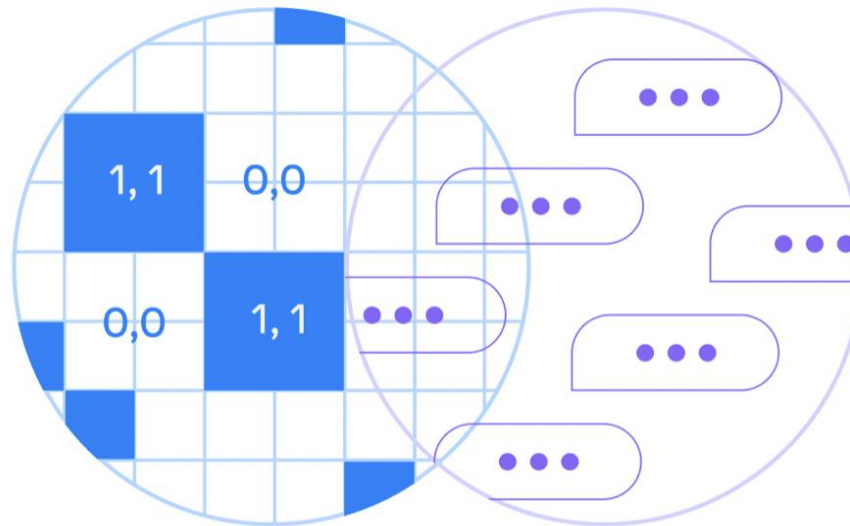
Meta AI presents CICERO — the first AI to achieve human-level performance in Diplomacy, a strategy game which requires building trust, negotiating and cooperating with multiple players.

Learn more about #CICERObyMetaAI: bit.ly/3GBwLzx



3. Cicero: “Free Energy” for a Game Theory of Mind II

The game of “Diplomacy” and the AI Cicero that learned to play like a human



Strategic Reasoning

CICERO predicts the moves other players are likely to make, as well as what moves they expect CICERO to make, and uses that information to create a strategic plan.

Natural Language Processing

CICERO grounds its conversations in a set of carefully chosen plans, so it can negotiate, offer advice, share information, and make agreements with other players.

3. Cicero: “Free Energy” for a Game Theory of Mind II

The game of “Diplomacy” and the AI Cicero that learned to play like a human

Example of coordination - CICERO is AUSTRIA

ITALY: What are you thinking long term?
Should I go for Turkey or head west

AUSTRIA: Yeah, he went to Armenia which is really great. You can go either way, but if Turkey is committing to Russia you could always lepanto

AUSTRIA: A lepanto into Turkey is really really strong, especially since he committed so hard against Russia

ITALY: I'm down to go for it. Would definitely need your help in O2 though

AUSTRIA: Of course, happy to do that!

ITALY: Fantastic!

Fig. 6. Successful dialogue examples.

3. Cicero: “Free Energy” for a Game Theory of Mind II

The game of “Diplomacy” and the AI Cicero that learned to play like a human

What does Meta AI’s Diplomacy-winning Cicero Mean for AI?

Hint: It’s not all about scaling



Gary Marcus and Ernest Davis
Nov 26

♡ 45

💬 21



“The distinguishing property of humans is to search for and to follow after truth.”

– Cicero

3. Cicero: “Free Energy” for a Game Theory of Mind II

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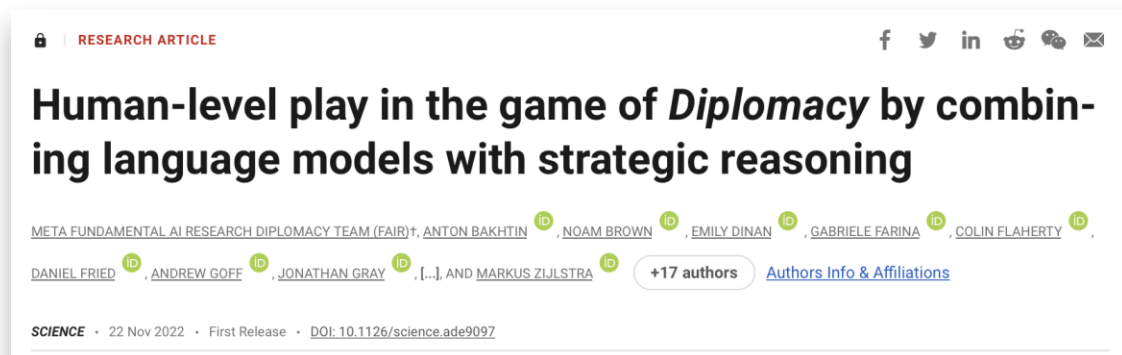


“The distinguishing property of humans is to search for and to follow after truth.”

– Cicero

Diplomacy, a complex game that requires extensive communication, has been recognized as a challenge for AI for at least fifty years. To win, a player must not only play strategically, but form alliances, negotiate, persuade, threaten, and occasionally deceive. It therefore presents challenges for AI that are go far beyond those faced either by systems that play games like Go and chess or by chatbots that engage in dialog in less complex settings.

3. Cicero: “Free Energy” for a Game Theory of Mind II



piKL: KL-regularized planning

piKL assumes player i seeks a policy π_i that maximizes the modified utility function

$$U_i(\pi_i, \pi_{-i}) = u_i(\pi_i, \pi_{-i}) - \lambda D_{KL}(\pi_i \parallel \tau_i) \quad (1)$$

where π_{-i} represents the policies of all players other than i , and $u_i(\pi_i, \pi_{-i})$ is the expected value of π_i given that other players play π_{-i} . Specifically, let $Q_i^{t-1}(a_i) = u_i(a_i, \pi_{-i}^{t-1})$ and let

$$\pi_i^{At}(a_i) \propto \tau_i(a_i) \exp\left[\frac{Q_i^{t-1}(a_i)}{\lambda}\right] \quad (2)$$

On each iteration t , piKL updates its prediction of the players' joint policies to be

$$\pi^t = \left(\frac{t-1}{t}\right) \pi^{t-1} + \left(\frac{1}{t}\right) \pi^{At} \quad (3)$$

3. Cicero: “Free Energy” for a Game Theory of Mind II



Cisero's equivalent of Free Energy is:

$$U(\pi_i, \pi_{-i}) = u(\pi_i, \pi_{-i}) + \lambda D_{KL}(\pi_i | \tau_i) \quad (12)$$

$$= u(\pi_i, \pi_{-i}) + \lambda \underbrace{\left(\underbrace{-H(\pi_i)}_{\text{Entropy}} + \underbrace{H(\pi_i, \tau_i)}_{\text{cross entropy}} \right)}_{\text{Log-loss game}} \quad (13)$$

$$= \overbrace{u(\pi_i, \pi_{-i}) + \lambda \left(\underbrace{-H(\pi_i)}_{\text{Entropy}} + \underbrace{H(\pi_i, \tau_i)}_{\text{cross entropy}} \right)}^{(\text{local}) \text{ MaxEnt Game Theory}} \quad (14)$$

3. Cicero: “Free Energy” for a Game Theory of Mind II

The takeaway for this section:

- Successful strategically interacting AIs are using a (simple) form of ToM
- Strategy is only one part of the solution
- Also need a language model, a filter, and human fine-tuning of opening gambit
- Requires grounding in an “objective” world
- And ... only 1 player suspected they were interacting with an AI

4. Some Consequences of AI and ToM based Social Interactions

4. Some Consequences of AI and ToM based Social Interactions

Inverse Reinforcement Learning as the Algorithmic Basis for Theory of Mind: Current Methods and Open Problems

by  Jaime Ruiz-Serra  and  Michael S. Harré *  

Modelling and Simulation Research Group, School of Computer Science, Faculty of Engineering, The University of Sydney, Sydney, NSW 2006, Australia

* Author to whom correspondence should be addressed.

Algorithms **2023**, *16*(2), 68; <https://doi.org/10.3390/a16020068> (registering DOI)

Received: 16 December 2022 / Revised: 13 January 2023 / Accepted: 16 January 2023 /

Published: 19 January 2023

4. Some Consequences of AI and ToM based Social Interactions

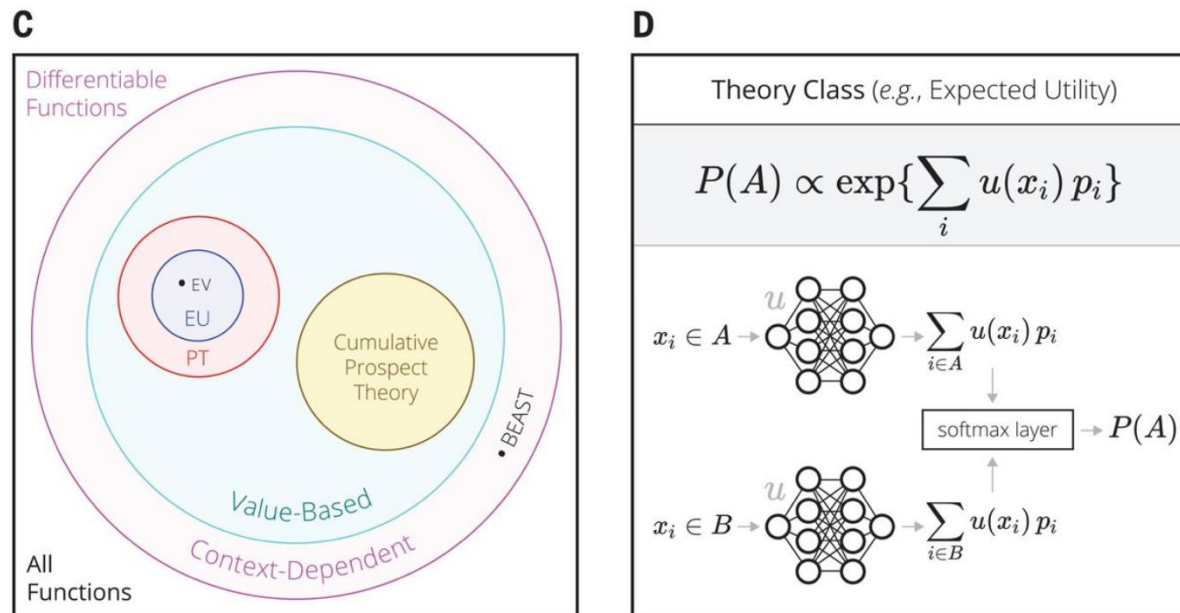


Fig. 1 Applying large-scale experimentation and theory-driven machine learning to risky choice.

4. Some Consequences of AI and ToM based Social Interactions

Theory of Mind is only one aspect

- Cicero has a complex, integrative, architecture
- Scaling up an AI doesn't give us ToM by default: AI scaling hypothesis is probably wrong
- The human brain is modular with interacting functions



The modular and integrative functional architecture of the human brain

Maxwell A. Bertolero^{a,b,1}, B. T. Thomas Yeo^{c,d,e,f}, and Mark D'Esposito^{a,b}

^aHelen Wills Neuroscience Institute, University of California, Berkeley, CA 94720; ^bDepartment of Psychology, University of California, Berkeley, CA 94720; ^cDepartment of Electrical and Computer Engineering, National University of Singapore, Singapore 119077; ^dClinical Imaging Research Centre, National University of Singapore, Singapore 117599; ^eSingapore Institute for Neurotechnology, National University of Singapore, Singapore 117456; and ^fMemory Networks Programme, National University of Singapore, Singapore 119077

Edited by Michael S. Gazzaniga, University of California, Santa Barbara, CA, and approved October 23, 2015 (received for review May 29, 2015)

"... we find a strong spatial correspondence between the cognitive functions and the network's modules, suggesting that **each module performs a discrete cognitive function**. Crucially, **activity at local nodes** within the modules **does not increase in tasks that require more cognitive** functions, demonstrating the autonomy of modules' functions. However, **connector nodes do exhibit increased activity when more cognitive functions are engaged** in a task."

4. Some Consequences of AI and ToM based Social Interactions

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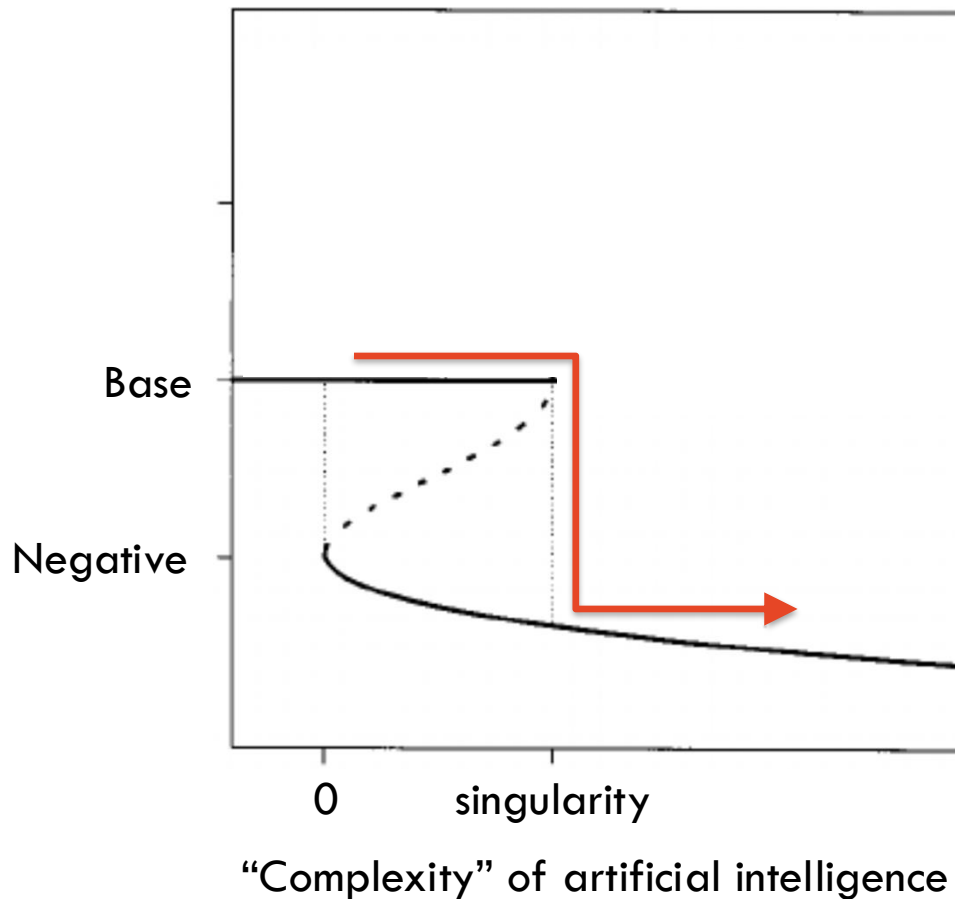
Collective minds: social network topology shapes collective cognition

Ida Momennejad 

Published: 13 December 2021 | <https://doi.org/10.1098/rstb.2020.0315>

4. Some Consequences of AI and ToM based Social Interactions

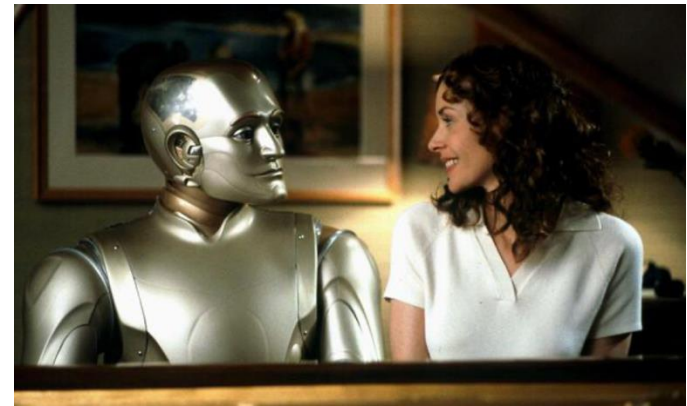
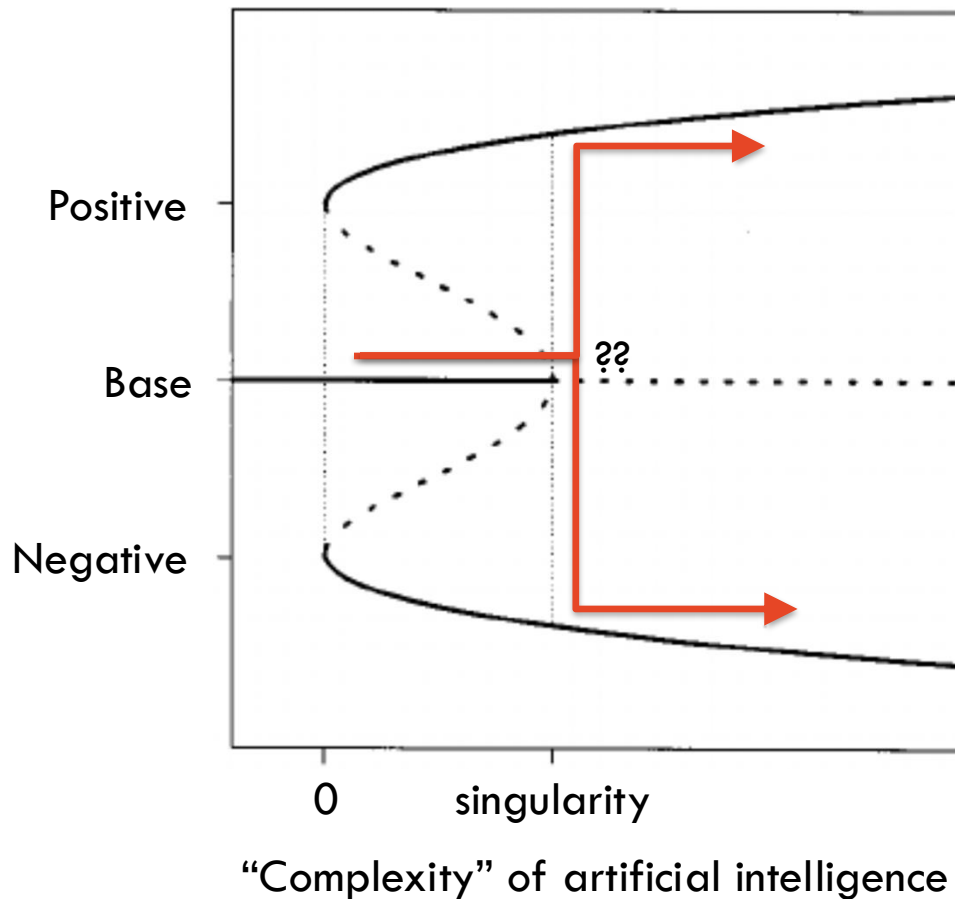
The pessimist view



I, Robot (2004, 20th Century Fox)

4. Some Consequences of AI and ToM based Social Interactions

A bet both ways: “Sensitive intervention points” (J.D. Farmer et al, 2019)



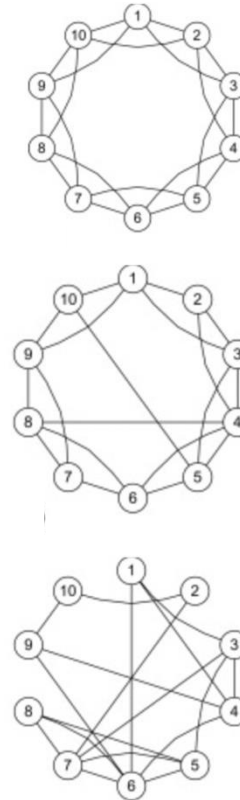
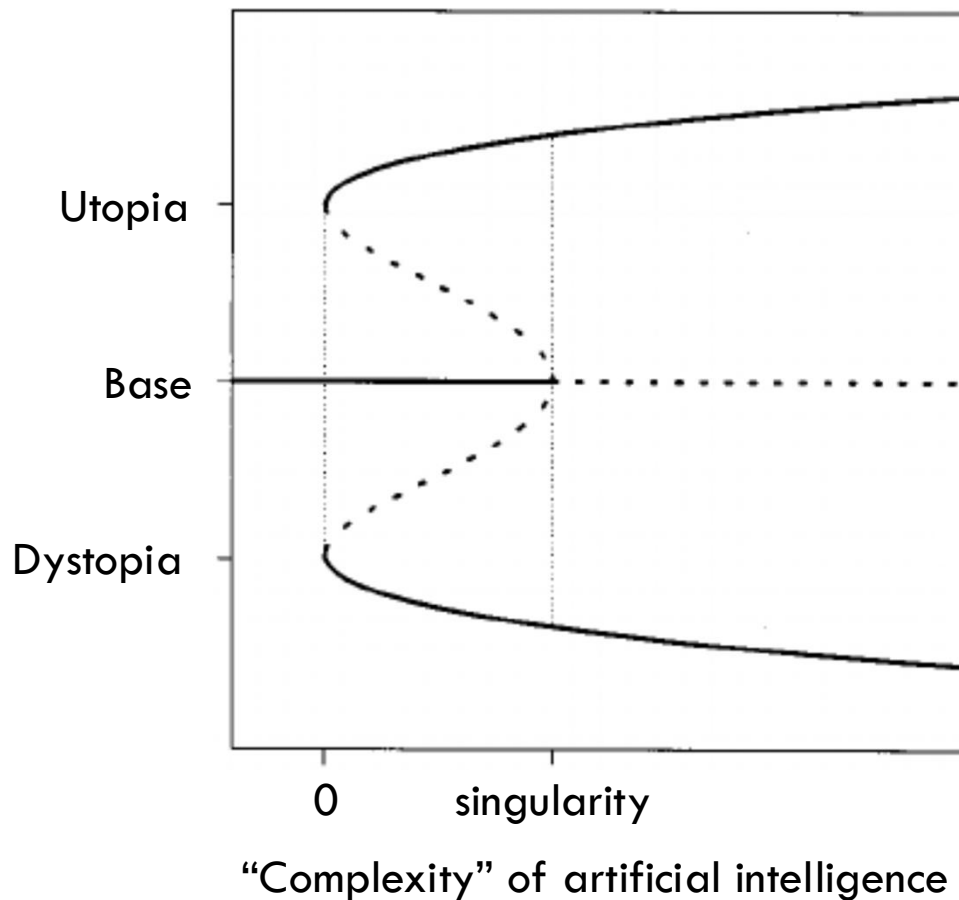
Bicentennial Man (1999 , Touchstone Pictures)



I, Robot (2004, 20th Century Fox)

4. Some Consequences of AI and ToM based Social Interactions

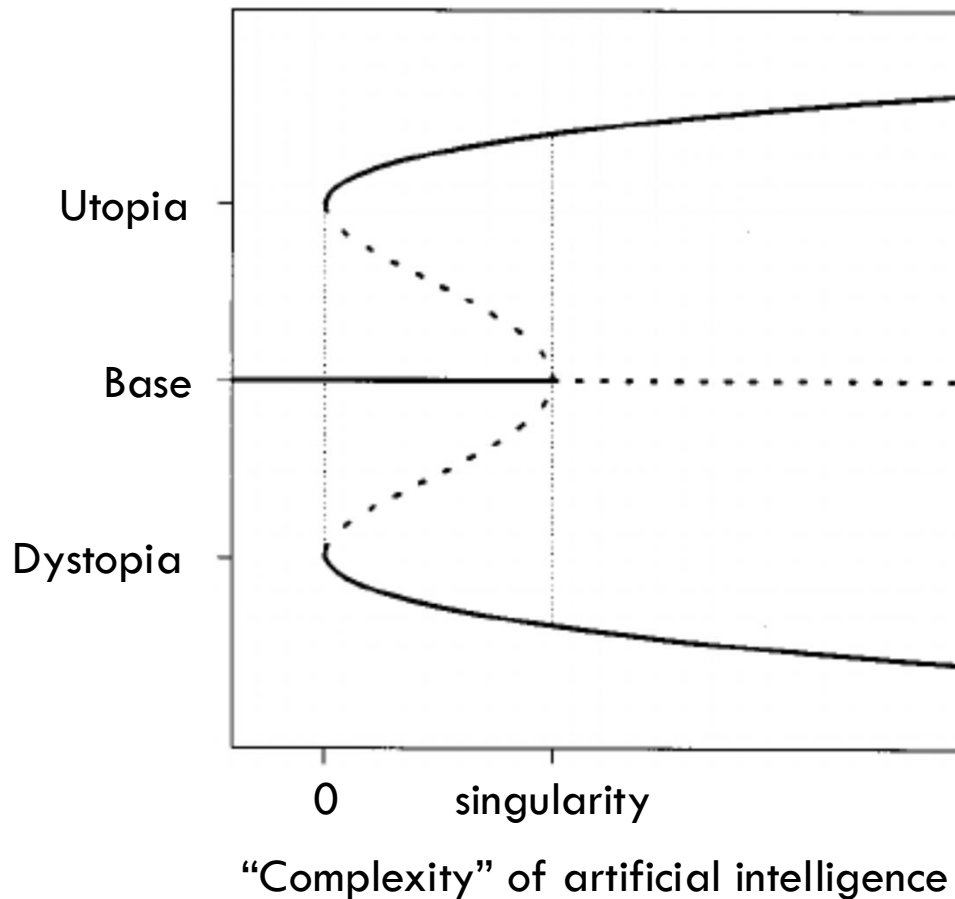
A bet both ways: “Sensitive intervention points” (J.D. Farmer et al, 2019)



Same agents,
different relationships,
different global outcomes

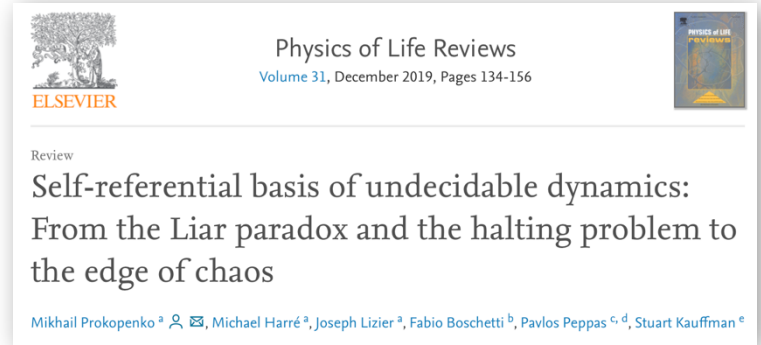
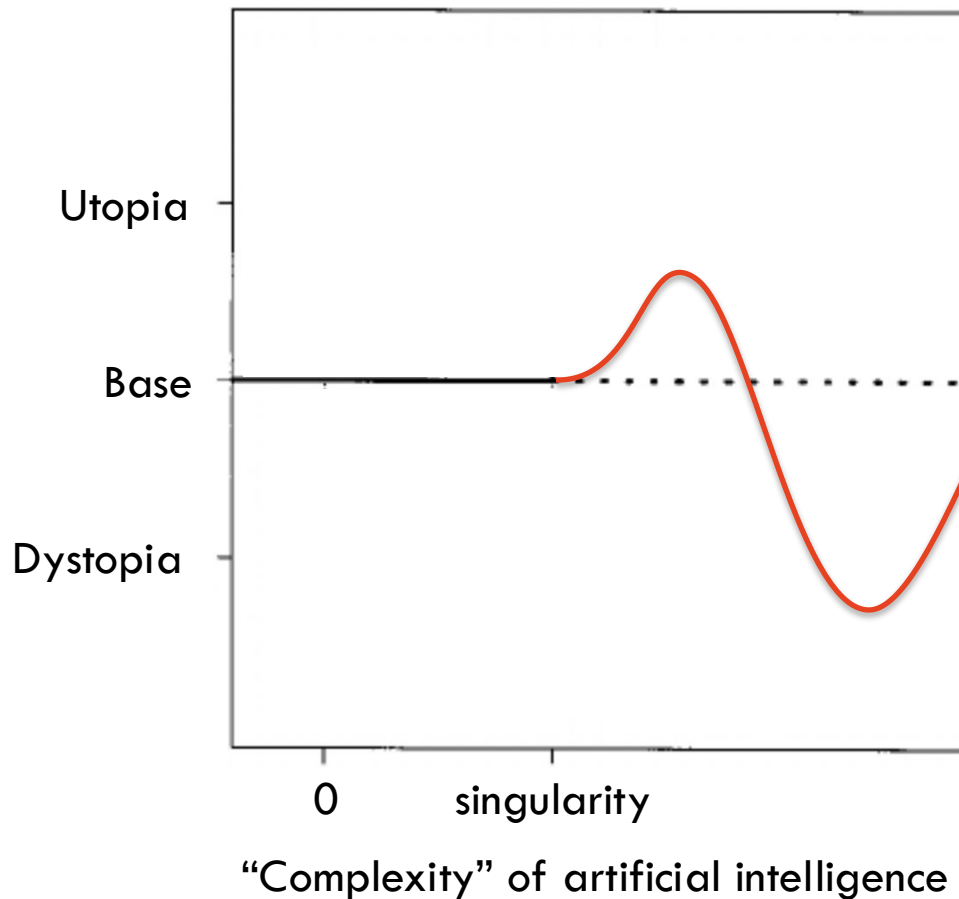
4. Some Consequences of AI and ToM based Social Interactions

A bet both ways: “Sensitive intervention points” (J.D. Farmer et al, 2019)



4. Some Consequences of AI and ToM based Social Interactions

The future is weird (not computable)



4. Some Consequences of AI and ToM based Social Interactions



Physics of Life Reviews
Volume 31, December 2019, Pages 134-156



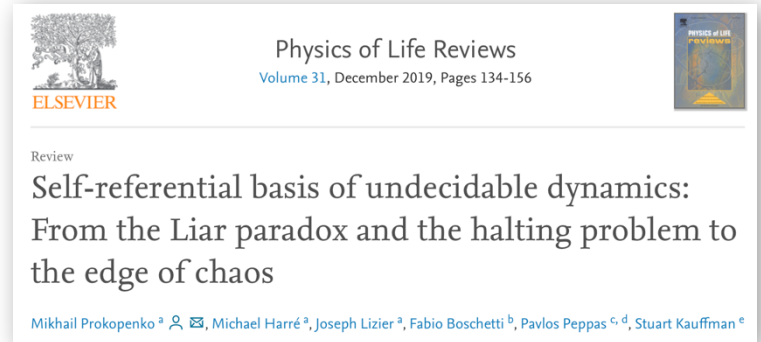
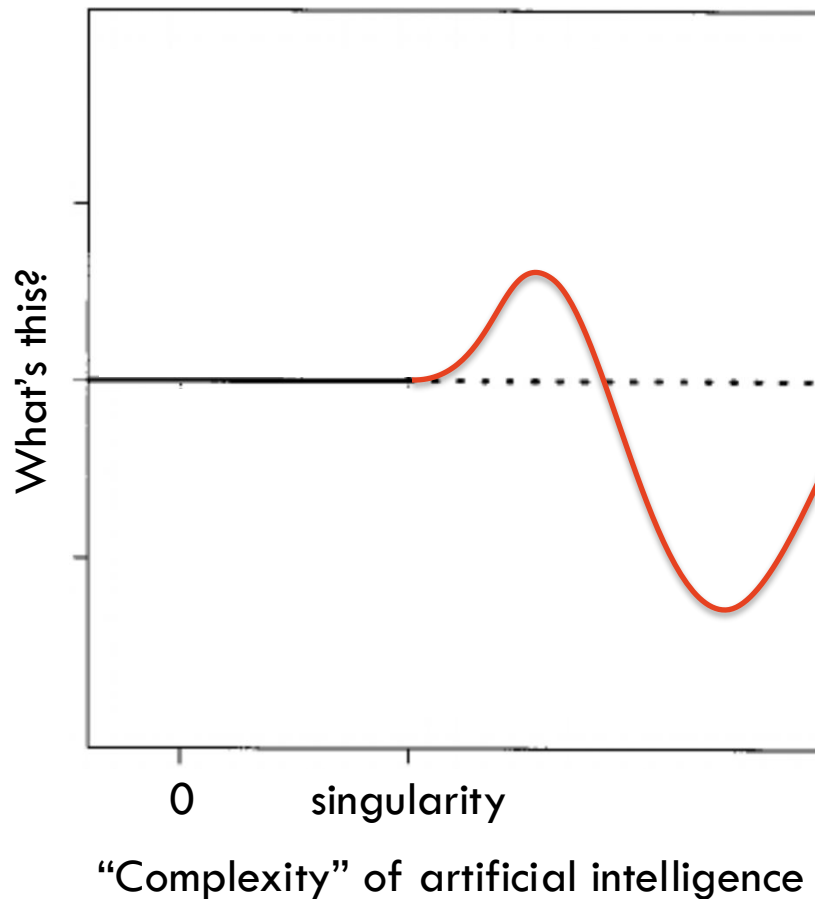
able dynamics:
altating problem to

ti^b, Pavlos Peppas^{c, d}, Stuart Kauffman^e



4. Some Consequences of AI and ToM based Social Interactions

The future is weird (not computable)



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Questions



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